# The Algorithm of Urban Estates Valuation 

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## Urban Real Estates

- Urban real estates definition
- Specific parameters
- The estates' prices registration in Poland


## VALUATION MODEL PARAMETERS'

 ESTIMATION $C_{T j}=S_{1} \times c_{1}+S_{2} \times c_{2}+\ldots+S_{i} \times c_{i}+a_{1} \times k_{1}+\ldots+a_{s} \times k_{s}$- $C_{T j}$ - transaction price for whole j-estate,
- $S_{i}$ - the area of every i-element (parcel, parcel parts having defined soil classes, flat or building usable areas or whole building),
- i-element unit price,
- $a_{1}, a_{2}, \ldots . . . a$-attributes accepted for urban estates estimation values,
- $k_{1}, k_{2}, \ldots, \ldots, .$, the weight coefficients of attributes accepted for urban estates valuation


## VALUATION MODEL PARAMETERS' ESTIMATION

$$
\left\{C_{r}\right\}=\{[S] \quad[a]\} \cdot\left\{[[c]\}+\left\{\delta_{r}\right\}\right.
$$

## VALUATION MODEL PARAMETERS' ESTIMATION

- The estimators of vector $[\hat{c}]$ and vector [ $\hat{\text { may }}$ ] be written as following block matrices:
- $\left\{C_{T}\right\}$ - transaction prices vector, for whole estates,
- [S]- rectangular vertical matrix, containing areas of elements for elaborated estates
- $[a]$ - rectangular vertical matrix, containing attributes of elaborated urban estates
- $\{c\}$-unit prices coefficients vector for estates' elements,
- [k]-weight coefficients vector for elaborated attributes,
- $\quad$ - vector of random remainder (differences between transaction prices and model values).

VALUATION MODEL PARAMETERS ESTIMATION
$\left\{\hat{\delta}_{T}\right\}=\left\{C_{T}\right\}-\{[S] \quad[a]\} \cdot\left\{\begin{array}{l}{[\hat{c}]} \\ {[\hat{k}]}\end{array}\right\}$

## VALUATION MODEL PARAMETERS' ESTIMATION

- The covariance matrix of estimated parameters may be written in formula



## VALUATION MODEL PARAMETERS' ESTIMATION

- After performing the analysis of variance for transaction prices vector for the whole estates, we may find the covariance matrix of $\{\hat{\delta}\}$ vector. It has the following form


## THE VALUATION OF MARKET VALUE FOR URBAN ESTATES

- The estimated market value of elaborated urban estate can be expressed by the formula below

- The variance of estimated market value for urbanized estate can be defined including covariance matrix as follows


## THE EXAMPLES OF URBAN ESTATES' <br> VALUATION

The application of valuation parametric model will be presented on the example of urban estates. Information from seven authenticated deeds obtained from public notaries was used here.
The following attributes has been taken into account during calculations:

-     - part of the city - suburbs,
-     - destination in land use city plan - the land of low urbanization intensification,
-     - localization - very good (2), good (1),
-     - access to parcel (estate)- good,
-     - vicinity - very good,
-     - public utilities - water, electricity, gas, sewage, road,
-     - standard of components used for building and decorating (building standard) - very high (2), high (1),
-     - usable area of urbanized buildings from $200 \mathrm{~m}^{2}$ to $340 \mathrm{~m}^{2}$,
-     - area of parcel from $810 \mathrm{~m}^{2}$ to $1050 \mathrm{~m}^{2}$.


## THE EXAMPLES OF URBAN ESTATES VALUATION

There are seven urban real estates that were chosen for consideration. They description and attributes are listed below.

1. Built up estate with commercial building. Building usable area is $260 \mathrm{~m}^{2}$. Parcel area is $850 \mathrm{~m}^{2}$. Attributes: localization - very good (2), building standard - high (1), price $1570000 \mathrm{zl}(402000$ EUR 1 EUR $=3.9 \mathrm{zt})$
2. Built up estate with commercial building. Building usable area is $300 \mathrm{~m}^{2}$. Parcel area is $970 \mathrm{~m}^{2}$. Attributes: localization - good (1), building standard - high (1), price 1600000 zt (410 000 EUR)
3. Built up estate with commercial building. Building usable area is $220 \mathrm{~m}^{2}$. Parcel area is $760 \mathrm{~m}^{2}$. Attributes: localization - very good (2), building standard - very high (2), price 1450000 zf ( 372000 EUR)
4. Built up estate with commercial building. Building usable area is $320 \mathrm{~m}^{2}$. Parcel area is $910 \mathrm{~m}^{2}$. Attributes: localization - very good (2), building standard - high (1), price 1800000 zł (462 000 EUR)
5. Built up estate with commercial building. Building usable area is $200 \mathrm{~m}^{2}$. Parcel area is $810 \mathrm{~m}^{2}$. Attributes: localization -good (1), building standard - high (1), price - 1200000 zt (308 000 EUR)
6. Built up estate with commercial building. Building usable area is $340 \mathrm{~m}^{2}$. Parcel area is $1050 \mathrm{~m}^{2}$. Attributes: localization - very good (2), building standard - high (1), price 1900000 zł (487 000 EUR)
7. Built up estate with commercial building. Building usable area is $290 \mathrm{~m}^{2}$. Parcel area is $880 \mathrm{~m}^{2}$. Attributes: localization - good (1), building standard - high (1), price 1570000 zł (397 000 EUR)

## The estimation of valuation model's

## parameters

- The information obtained from deeds is basis for 7 equations written according to the formulas presented before. Every equation has two price coefficients and two weight coefficients. The matrix [S] of parcel areas and building usable areas and the matrix [a] of market attributes and the matrix $\left\{\mathrm{C}_{\mathrm{T}}\right\}$ of transaction prices have the following form:

1570000
1600000
1600000

## The estimation of valuation model's parameters

From the estimation of this model's parameters according to formulas presenting unit prices coefficients and random remainders calculated for every transaction, were obtained. The unit parcel and urban buildings' prices coefficients are as follows:
$\hat{c}_{G}=349,43 \mathrm{z} / / \mathrm{m}^{2}$

## The estimation of valuation model's parameters

- The covariance matrix obtained for all estimated parameters consists of the following values

$$
\operatorname{Cov}\left\{\left[\begin{array}{l}
{[\hat{c}]} \\
{[\hat{k}]}
\end{array}\right\}=1657,983\left[\begin{array}{cccc}
31.02 & -92.34 & 1561.85 & -3856.94 \\
1-1 & 295.00 & -7277.59 & 10584.97 \\
1-1 & 1 & 898922.81 & -695651.17 \\
1 & 1 & 1
\end{array}\right]\right.
$$

## The valuation of similar estates

- As a subject of valuation we choose estate similar to estates elaborated in market analysis presented above. This is the commercial estate, that has usable area of $260 \mathrm{~m}^{2}$. This parcel has an area of $980 \mathrm{~m}^{2}$. The localization is good (1) and building standard high (1). Applying formula we obtained estates market value stands as follows:


## The valuation of similar estates

- After performing operation on the proper matrices, the standard deviation of estimated market value was calculated. It is presented below:


The valuation of similar estates

- After applying Student distribution quantile, the symmetric confidence intervals for estimated estate's market value equal

$$
W \hat{R}=1468480 \pm 118765 z t
$$

