



Session 2.2: Gravity and WHS

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Session 2.2 Program

Précis: The gravity field is directly related to the structure of the Earth and how its mass is distributed. Every piece of mass creates a potential of gravity (geopotential) that drops off with distance. The cumulative effect of all these produces the Earth's gravity field. This session will focus on the relationship between various aspects of the Earth's gravity field such as the geoid, geopotentials, gravity, deflections of the vertical, and physical heights (e.g., above mean sea level). It covers different means of observing the gravity field and how they are combined to produce models for height determination both at global scales, such as the World Height System, and locally for National Vertical Datums.

- 1030 1100 Session 2.2: Gravity and WHS
- 1100 1130 Morning Tea and networking with Young Surveyors / Professionals
 Restaurant, Cassa Geometri Sponsored by Cassa Geometri
- 1130 1230 Continuation of Session 2.2: Gravity and WHS







Outline

- Introduction, outline, background: 5 slides
- Relationships between gravity, geopotential, DoV's & heights: 4 slides
- The gravity field spectrum -long wavelength, etc.: 4 slides
- Satellite gravity overview (GRACE/GOCE) 3 slides
 - Surface gravity (shipborne/land and relative/absolute): 2 slides
 - absolute meters: 2 slides
 - relative meters: 3 slides
 - − Surface surveys (terrestrial & shipborne) − 10 slides
- The Effect of Terrain (RTM's/TC's): 3 slides
- Altimetric Anomalies: Mapping the Oceans from Space: 4 slides
- Aerogravity: Bridging the gap between Satellites and Ground: 6 slides







Outline

- Deflection of the Vertical: the impact on IMU's: 1 slide
- Point estimates of geoid height: GNSS on leveling: 2 slides
- Tying it all together: EGM's: 3 slides
- Focusing on the local picture: Regional Models: 3 slides
 - World Height System vs. National Vertical Datums: 1 slide
- Using a Geoid model as a National Vertical Datum: 1 slide
- NAVD 88: the U.S. Vertical Datum: 3 slides
- Hybrid modeling using control data and a geoid: 4 slides
- Outlook for a future U.S. vertical datum: 1 slide
- Summary: 5 slides







Background

Dan Roman earned his Ph.D. at the Ohio State University and has been a Research Geodesist with the National Geodetic Survey since 1999. He is the team lead for Geoid Modeling and Research as well as the Principal Investigator for the Gravity for Redefinition of the American Vertical Datum (GRAV-D) Project. He developed GEOID99, GEOID03, GEOID06, GEOID09, and associated models.





Gravity, Geopotential & Heights

- Mass attracts other mass
- $M_E >>>$ any other mass
- Geopotential is 1/r
- Differential relationship
- Earth is more squashed
- So use *h* not *r*
- Then pick a datum (W_0)
- Physical heights relate to change in geopotential

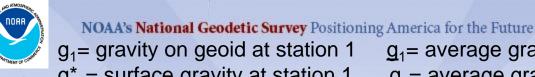
•
$$g = Gm_1m_2/r^2$$

- $g = GM (m)/r^2$
- W = GM m/r
- $g = \partial (W)/\partial r$
- geodetic not geocentric

•
$$g = \partial (W) / \partial h$$

$$^{\bullet} \qquad ^{0} \Delta C_{b-a} = \sum_{a}^{b} h_{i} g_{i}$$





www.ngs.noaa.gov

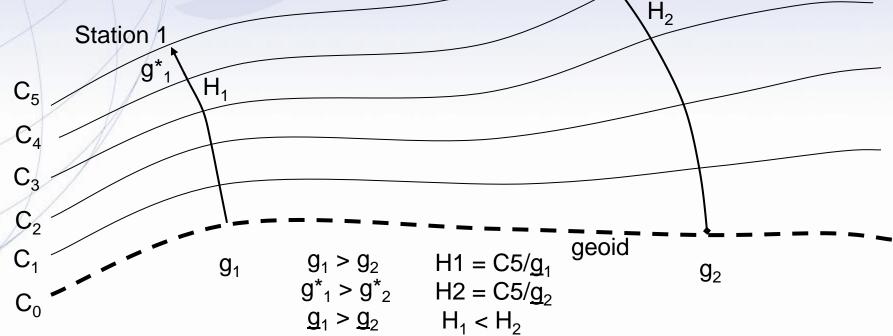
 g_1 = gravity on geoid at station 1 g_1 = surface gravity at station 1 g_2 = gravity on geoid at station 2 g_2 = surface gravity at station 2

g₂= surface gravity at station 2 H₁= orthometric height to station 1

H₂= orthometric height to station 2

 \underline{g}_1 = average gravity from g_1 to g_1^* \underline{g}_2 = average gravity from g_2 to g_2^*

Station 2



Note that surface location of station 1 is closer to the geoid than station 2. A steep gradient of geops indicates higher gravity – less steep indicates lower gravity. The geops being farther apart beneath station 2 to reflect lower local mass and gravity. Hence, H1 should be less than H2 – even though both have the same geopotential.







Gravity, Geopotential & Heights

- But the Earth is very big
- Best to remove most signal
- Need a good model: GRS80 It fits better than 99%
- Work with residual values
- Residual = actual model

Disturbing Potential

 $T = W_P - V_P$

Gravity anomalies

 $\Delta g = g_P - \gamma_O = \partial (T) / \partial h - 2T/h$

- Bruns Formula

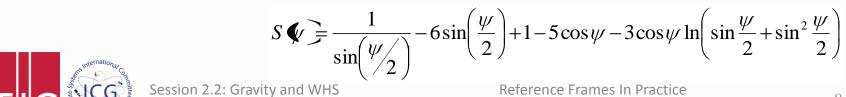
N = T/g

Height relationships

h = H + N

- Stokes' Formula

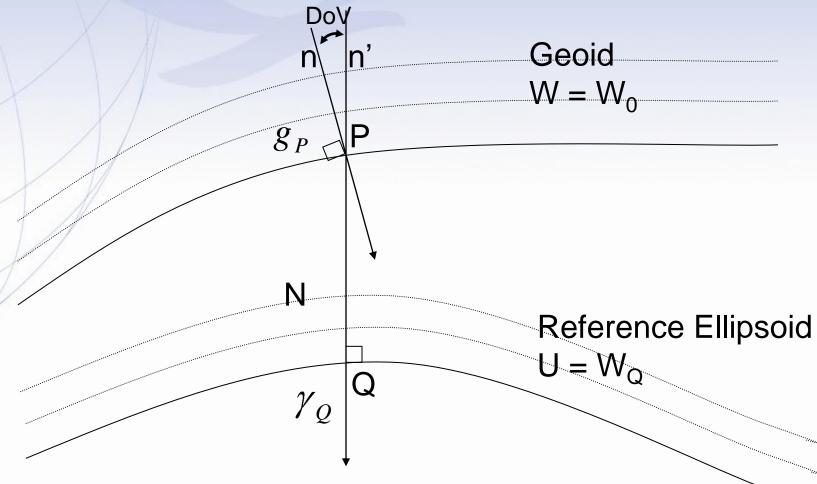
 $N = \frac{R}{4\pi G} \iint_{\sigma} \Delta g S \, \mathbf{V} \, \mathbf{d}\sigma$







Gravity, Geopotential & Heights



From Figure 2-12, p.83 of Heiskanen and Moritz, 1967, Physical Geodesy







The Gravity Field Spectrum

- Concepts of scale
 - Long wavelengths: satellites
 - Short wavelengths: terrain
- Degree-Spectrum plot
 - Satellite gravity models
 - Aerogravity
 - Surface gravity observations
 - Terrain modeled gravity







What does long wavelength mean?

Satellite's orbit



altitude is usually many 100's of km

Observed gravity anomalies







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What does short wavelength mean?

Dealing with residuals

- gravity anomalies
- $\Delta g = g_{\rm P} \gamma_{\rm Q}$
- Most signal removed (γ)
- Accounts for degree 2
- Leaves everything else
- Satellite models > 200 km
- Terrestrial gravity coverage not likely sufficient
- Must use DTM/DEM's

Dealing with mountains

- Residual Terrain Model
 - Models the terrain in SHM/EHM
 - Used in EGM2008 to 5'
 - Use SRTM 3" to get 3"-5"
 - 90 meter resolution
 - Signal < 3" affects Δg 's
- **Terrain Corrections**
 - Used more with Stokes approach
 - Removes impact on gravity obs.
 - Then you make the geoid model



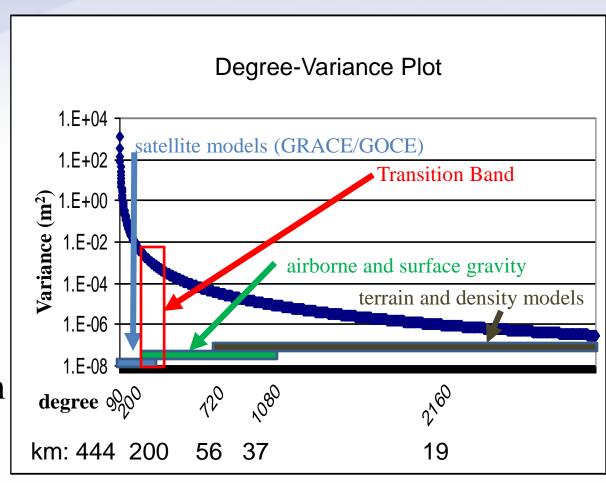






The Gravity Field Spectrum

- SHM/EHM
- Inverse to scale
- d. 2 => Ellipsoid
 - 2 oscil. in circle
- Earth is 40,000 km round
- d. 360 is 1/360th of that or 111 km
- d. 2160 is 18 km











Satellite Geodesy

- Started with tracking satellites in orbit (60's)
- First dedicated gravity mission was CHAMP
- GRACE was next (10 years on and still going)
- GOCE flying (20 months)
- Likely GRACE II/GFO & follow-on ESA missions

- Best approaches involve
 - GNSS receivers: hi-low
 - Low-low tracking (GRACE)
- Basic idea: orbital changes arise from gravity changes
- NOTE: gravity is observed in orbit <u>not</u> on the ground
- Also, orbital height is a function of sensitivity to scale (attenuation)

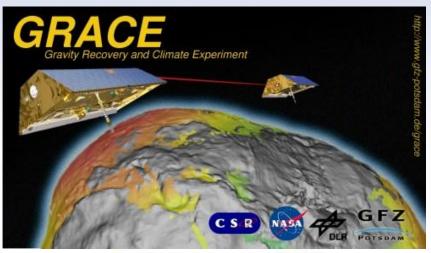


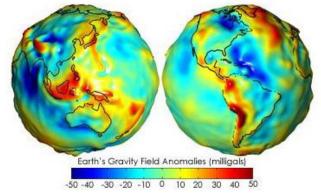
NOAA's National Geodetic Survey Positioning America for the Future

SURVEY SURVEY

Gravity Recovery and Climate Experiment (GRACE)

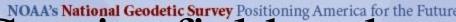
- PI's are Tapley (CSR U. of Texas) and Reigher (GFZ)
- Dual Satellites
 - Orbital tracking (350 km)
 - Satellite-to-Satellite (lo-lo, hi-lo)
- Polar orbit solves for deg. 2
 - Previous solution gap > 83
 - Solutions to deg. 120
 - Generally accepted to deg. 60-90
- Serves as base level for global gravity & geoid height models





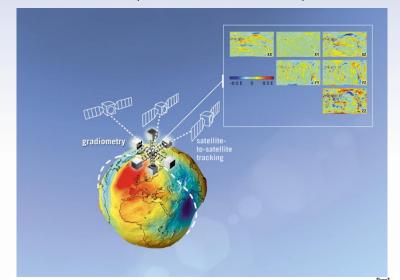
http://www.csr.utexas.edu/grace/

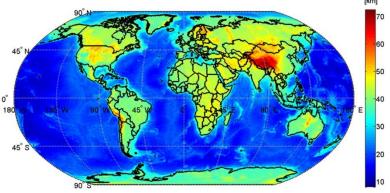




Gravity field and steady-state Ocean Circulation Explorer (GOCE)

- Mission Scientists: Drinkwater & Haagmans
- 3x Accelerometer pairs
 - Determines gradient $(\Delta(\Delta W))$
 - Used to integrate Δg to surface
- Orbital tracking (260 km)
 - Satellite is compact & heavy
 - Short life expectancy (20 m.)
 - Resolves gravity to d.150 now
 - Ultimately will go to d. 200+







http://www.esa.int/SPECIALS/GOCE/index.html



From Satellite to Surface Gravity Observations

- Gravity meter types
- Surface gravity observations
- Examples from U.S data sets
 - Coverage/gaps
 - Systematic errors
 - Intra-survey errors
 - Inter-survey errors







Surface Gravity

- Absolute Meters (US\$500k or more)
 - Terrestrial only needs a lot of stability
 - National and international gravity networks
- Relative Meters (US\$100k-US\$1,000k)
 - Pendulums, springs with proof mass, SG
 - Uses: terrestrial, shipborne, airborne, & satellite
 - Most common type available and source of data
 - Yields difference in gravity between points





Absolute Gravity Meters

- Drop of proof mass (some are rise-fall tests)
- Interferometry of fringes to check acceleration
- Used to establish control for relative surveys
- Useful for work requiring extreme accuracy
- Manufacturers include
 - Micro-g LaCoste (Boulder, CO, USA)
 - Some academic & research models in development



Absolute Gravity Meters from

Micro-g LaCoste

http://www.microglacoste.com/absolutemeters.php

info@microglacoste.com

Meter	Accuracy	Precision	Repeatability	Temp Range	DC	AC	Outdoor Operation
	μGal	μGal/√(Hz)	μGal	C			
FG-L	10	100	10	15 to 30			
<u>A-10</u>	//10	100	10	-18 to +38			
<u>FG-5</u> (X)	2	15	1	15 to 30			















Relative Gravity Meters

- Original models include pendulum
 - Change in gravity proportional to change in period
- Other models include mass on spring, zerolength spring, & magnetically-suspended mass
- Manufacturers include
 - Micro-g LaCoste (Boulder, CO, USA)
 - Bell Geospace (Houston, TX, USA)
 - ZLS Corporation (Austin, TX, USA)







Relative Gravity Meters

- L & R Meter Service, LLC (Lexington, TX, USA)
- GWR Instruments, Inc. (San Diego, CA, USA) {SG}
- Neese Exploration (Haliburton) (Richmond, TX, USA)
- Fugro Gravity & Magnetics Services (worldwide)
- -<u>Sander Geophysics</u> (Ottawa, Ontario, Canada)
- Canadian Micro Gravity (Toronto, Ontario, Canada)





Relative Gravity Meters from Micro-g LaCoste

- Land Meters
 - LaCoste-Romberg
 - Scintrex CG-5



- Air/Sea Gravity System II
- Turnkey Airborne Gravity System
- System 6 Dynamic Gravity Meter









http://www.microglacoste.com/relativemeters.php









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Surface Gravity Surveys

Terrestrial

- Many different sources
- Uncertain corrections
- Potential for biases is big
- Individual surveys are generally smaller than the "state" level
- Better distribution generally
- Equipment
 - Portable g-meters
 - GPS or scaled from map

Shipborne

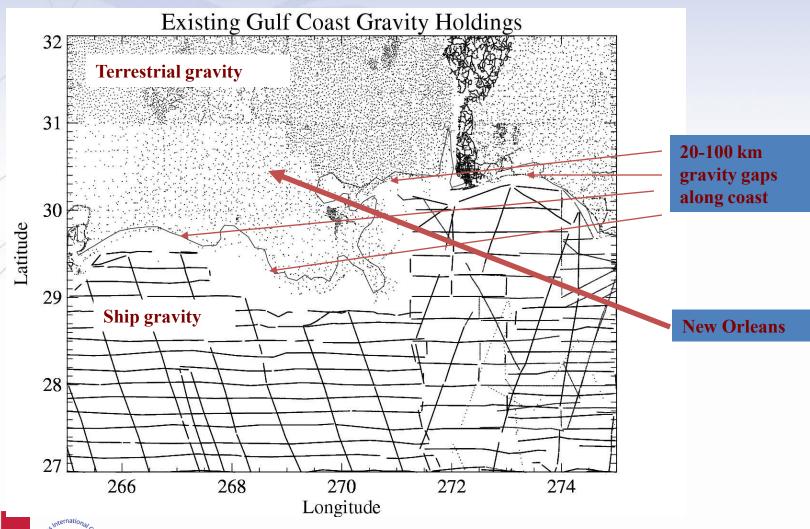
- Usually fewer sources
- More corrections required
- Internal consistency may be a problem (drift)
- Blown base ties can create huge systematic effect
- Greater sampling along track
- Equipment
 - Bell meter or Air/Sea II
 - GPS & IMU







Near Shore Data Gaps

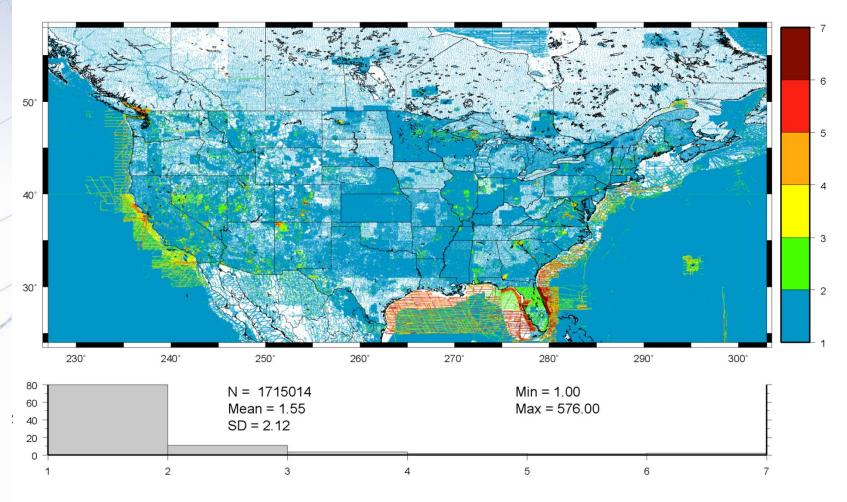








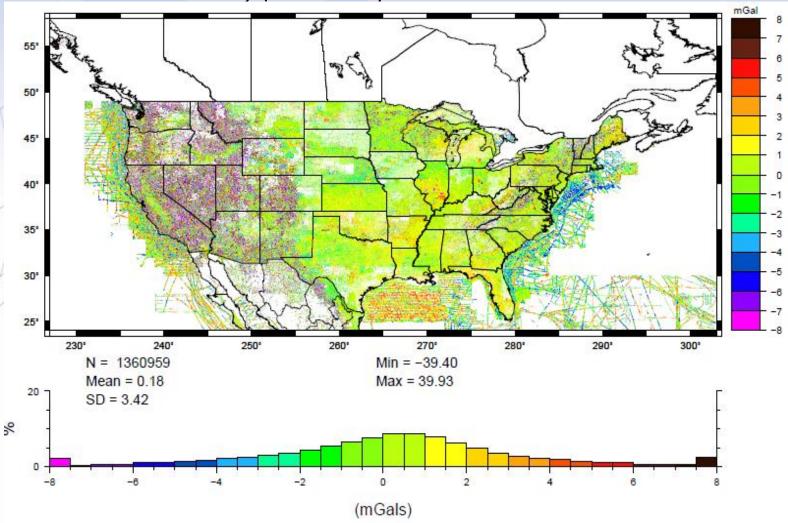
Number of Gravity Points Per 1x1 Minute cell







Residual gravity data for CONUS

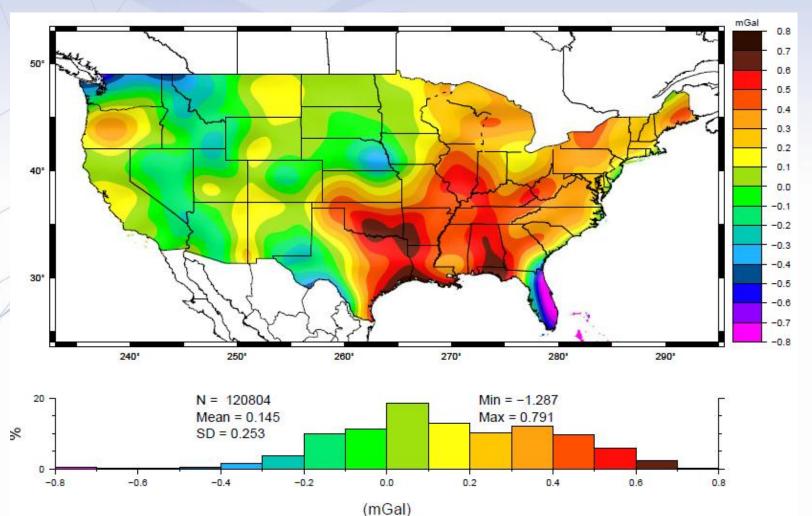








Long wavelength (deg 2-120) gravity errors

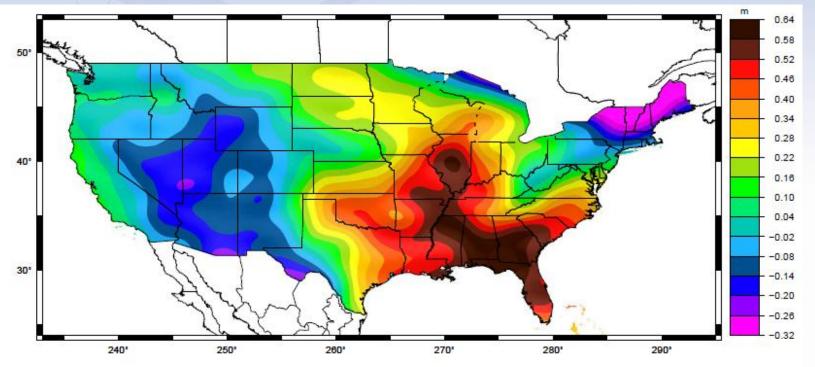


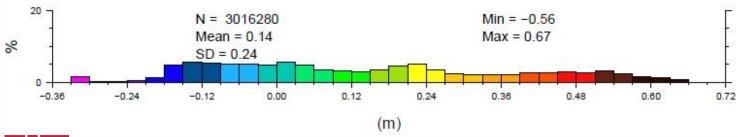






Long wavelength (deg 2-120) geoid errors











Surveys 2094 (red) and 4277 (green) The overlapping Surveys # 2094 (8425 obs.) and 4277 (22137 obs.) (4601 Crossovers)

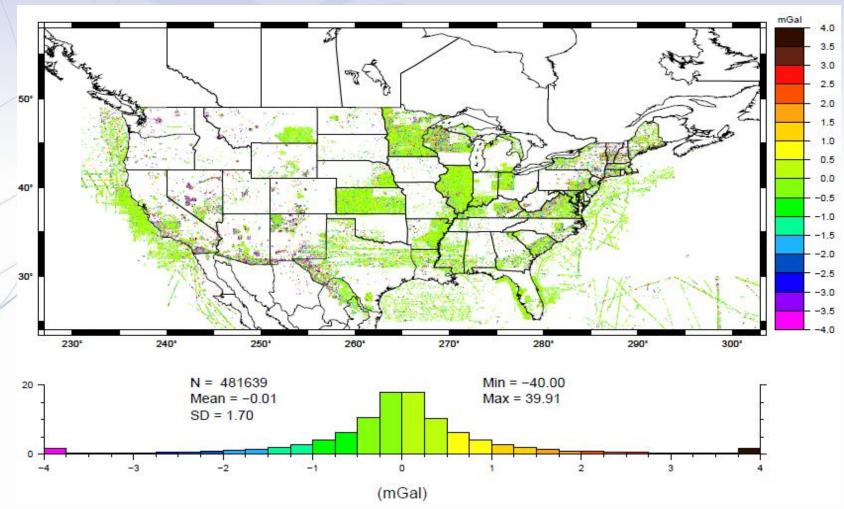
49° 48° 47° 46° 45° 263' 264° 265° 2611 266° 268° 269°







Internal Crossovers Between 1489 Surveys

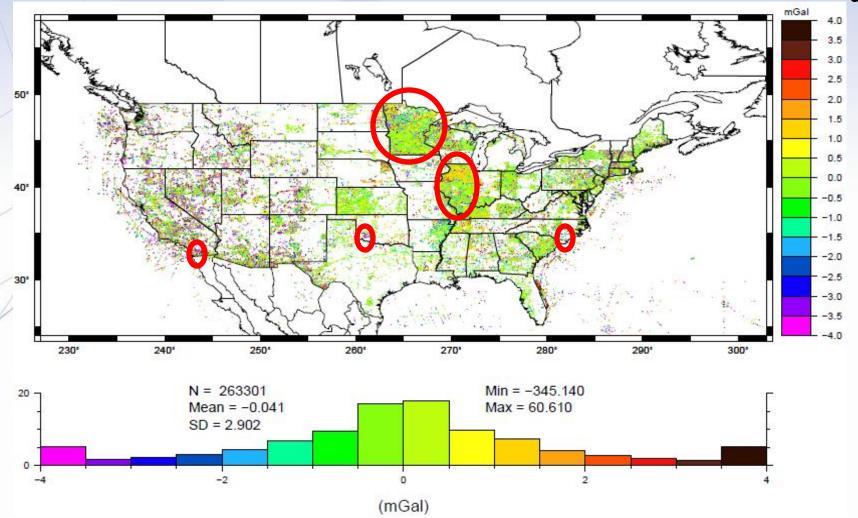








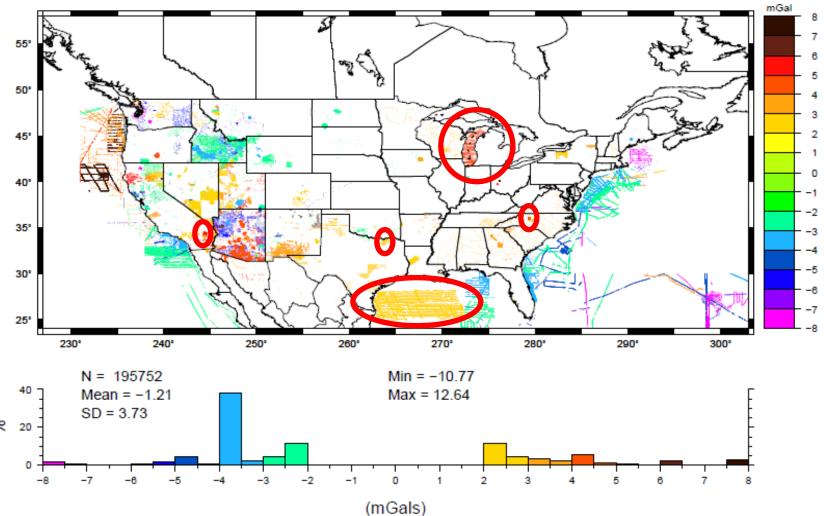
External Crossovers Between 1489 Surveys







244 Surveys with Significant Biases







The Effects of Terrain on the Short Wavelength (λ) Gravity Field

DEM/DTM/DTED

- Bare Earth model desirable
- Consistency is important too
- Sample interval varies
- Lidar is best but coverage is incomplete at national scale
- NED/CDED differences
- Satellites give near global coverage but may have gaps
- SRTM 3", ASTER, etc.

DDM

- Less significant than DEM's
- $\Delta \rho_{\text{rock/air}} >> \Delta \rho_{\text{rock/rock}}$
- Biggest impact: short λ
- Satellites capture long λ
- Most geodetic models use uniform density (ρ)
- DDM would provide better lateral/vertical variations







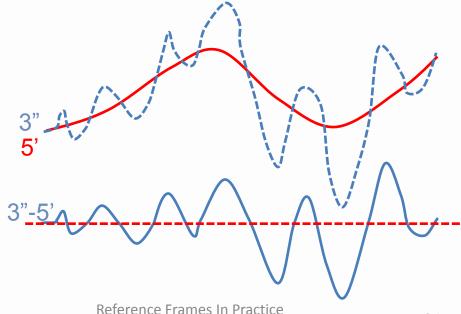
Residual Terrain Model (RTM)

General Concept

- Models the gravity effect of the variations in terrain
- Applied to gravity field model to remove effect
- EGM2008 has 5'- global
- Must account for more
- Not using 3"-5' RTM made 500,000 points too "noisy"
- Must develop residual RTM

3"-5' RTM Effects

- Interpolate 5' to 3" points
- Subtract for residual RTM









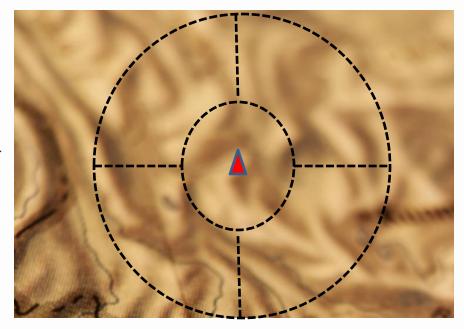
Terrain Corrections

General Concept

- Model the impact of terrain on gravity observations
- Correction is always positive
- A mountain will pull gravity vector towards it
- A canyon will deflect gravity vector away from it
- Net effects of both is to reduce observed gravity

Application

• Smoothes the gravity field for Helmert Condensation







Altimetric Anomalies

- Missions
 - GEOSAT
 - ERS-1/2
 - TOPEX/Poseidon
 - Jason
 - ICESAT
 - ENVISAT
 - ALTIKA
- Considerations
 - Radar signal/footprint

- Orbit uncertainties
- Maximum latitude
- Track spacing (orbit period)
- Ice or water returns
- Danish Products
 - DTU10
 - DNSC08
- Other Products
 - SIO
 - **– GSFC**00

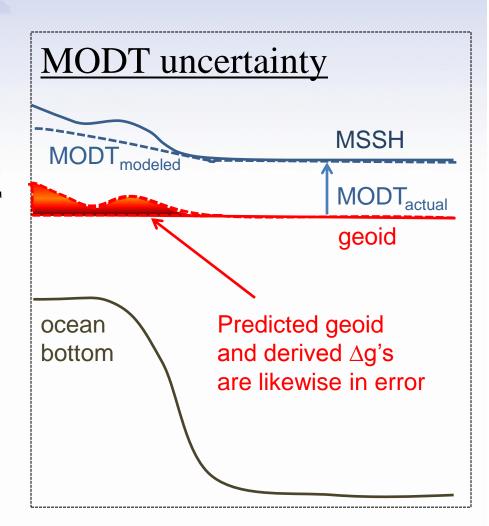




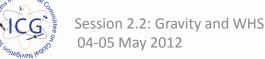


"Gravity" from an Altimeter

- Biggest assumption is that the MSSH can be used to estimate Δg 's
- MSSH = geoid + MODT
- MODT valid deep ocean
- Littoral regions poorly known (depths < 500m)
- Re-tracking may help MSSH but not MODT





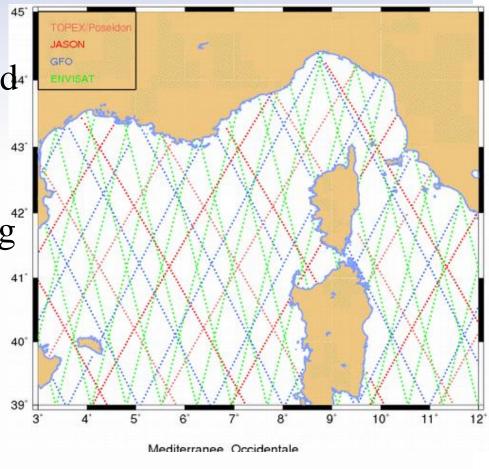






Altimeter Profiles

- Image from Centre of
 Topography of the Oceans and
 the Hydrosphere (CTOH)
- http://ctoh.legos.obs-mip.fr/
- Note disparity in track spacing 12
- Satellite orbits vary a lot
- SRTM only covered 60
- Most are sun-synchronous
 - 117 degree inclination => 83

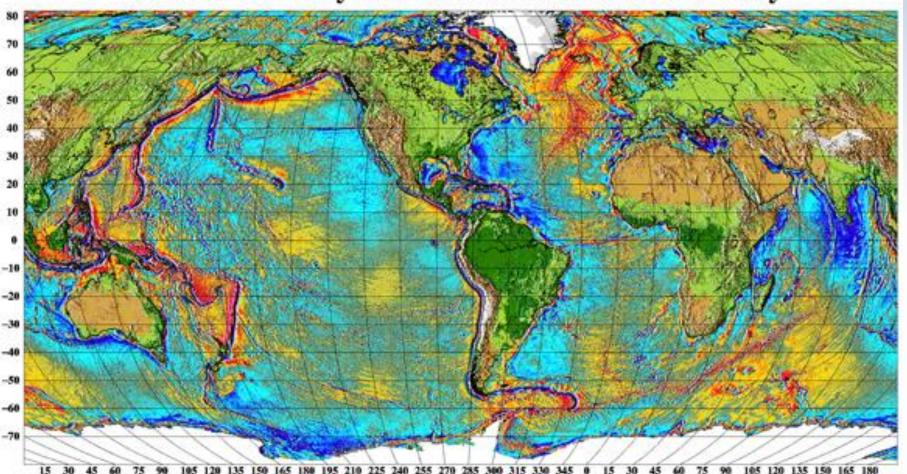








Free Air Gravity Anomalies from Satellite Altimetry



Andersen, O. B., P. Knudsen and P. Berry (2010) The DNSC08GRA global marine gravity field from double retracked satellite altimetry, Journal of Geodesy, Volume 84, Number 3, DOI: 10.1007/s00190-009-0355-9.







NOAA's National Geodetic Survey Positioning America for the Future Aerogravity: Bridging the gap between Satellites and Ground

- Satellite models provide long wavelength
 - 300 km and larger scales
 - Provide basis for unification
- Surface gravity data
 - Each observation contains total signal of Earth
 - Extent of gravity surveys covers maximum signal
- Aerogravity spans the other two
 - Determined by extent of survey (e.g., 20-500 km)







Other Benefits of Aerogravity

- Can span a greater territory than surface campaigns
- Can range over mountains and waterways easily
- Can connect different observational environments
 - terrestrial to shipborne to altimetric
- Can be fixed to satellite modeled gravity at long λ
- Can fix systematic errors in surface surveys (bias)
- Equipment, techniques, software, and procedures are already established and being refined

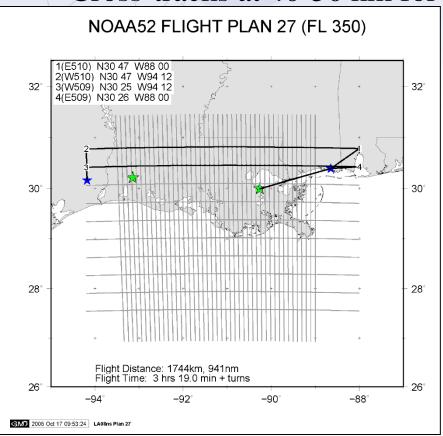


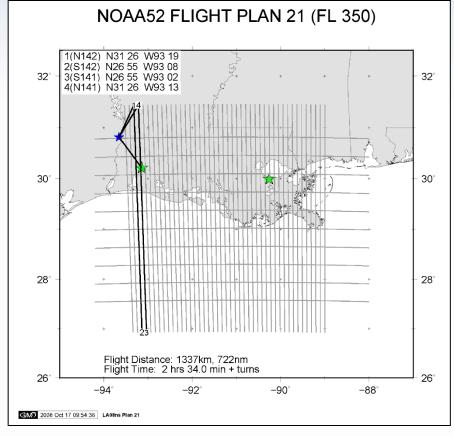




Flight Plans

- Data lines are 10 km apart
- Cross-tracks at 40-50 km for QC





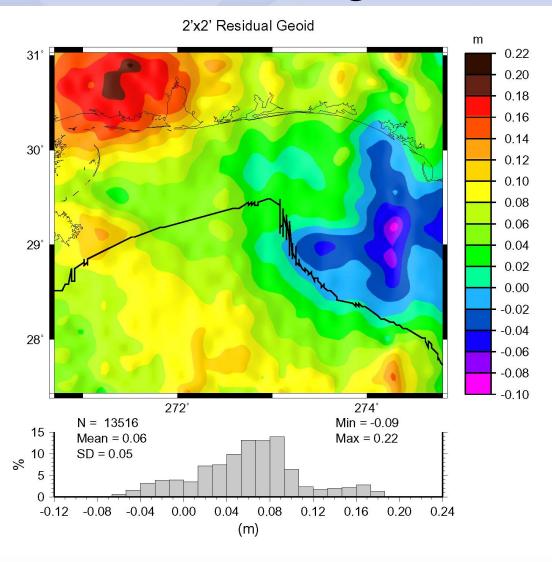








Implied Geoid Changes for GLS06



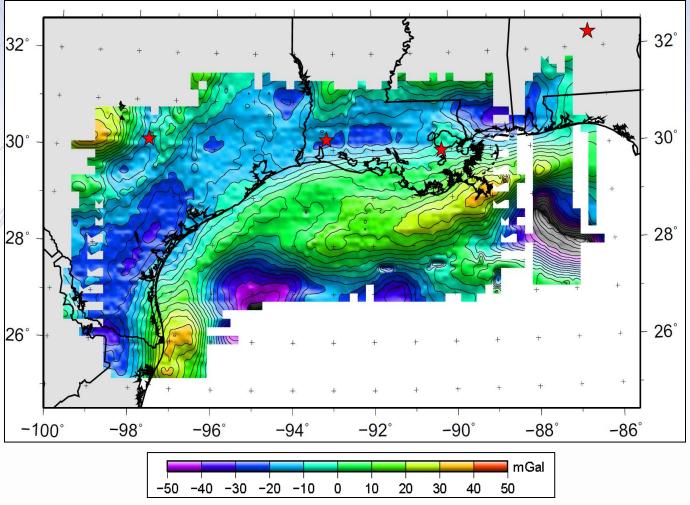








Survey for the western Gulf Coast







GRAV-D Coverage to date



Green: Available data and metadata

Blue: Data being processed, metadata may be available

White: Planned for data collection Orange: Data collection underway



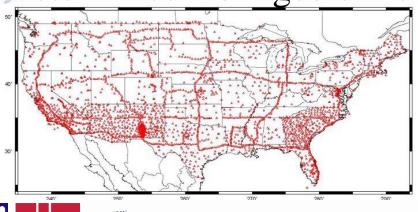


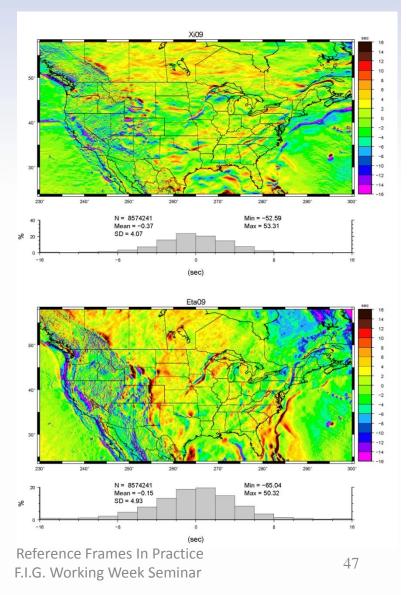




Deflection of the Vertical (DoV's)

- Another aspect of gravity field
- Angular difference of normals to ellipsoid and geoid
- Measured N-S (ξ) & E-W (η)
- Can help reduce drift in IMU's
- Determined from geoid model







Point Estimates of Geoid Height: GNSS/Leveling

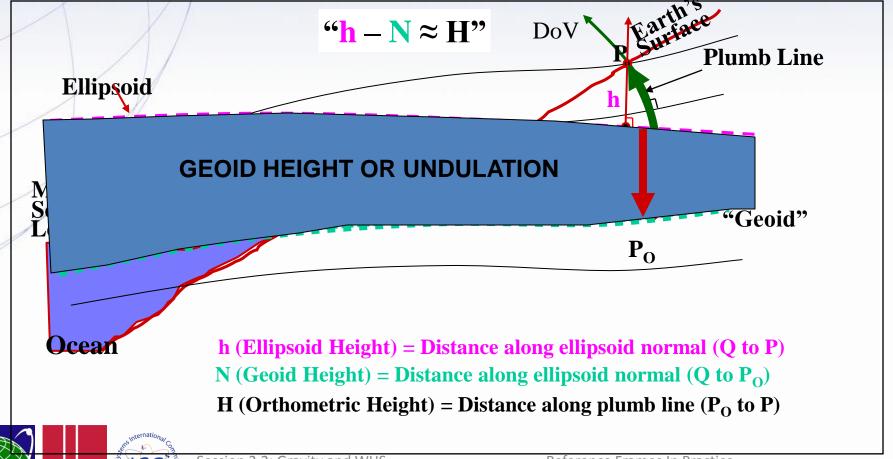
- This is, ultimately, the desired product
- However, these data will be sparse & irregular
- Care must be taken if these are combined in a single least squares adjustment with other functionals of the gravity field (e.g., Δg , ξ/η)
- Systematic effects must be guarded against
 - Is the vertical datum being used actually a geopotential surface?





SURVEY

Relationship between ellipsoid, geoid and orthometric heights.









Earth Gravity Models (EGM's)

- How to combine all these different data types?
- EGM's have accomplished this mostly:
 - EGM1996(EGM96)-produced by NIMA (NGA)
 - Problems in long wavelength (no GRACE/GOCE data)
 - Had to meld terrestrial solution with satellite (d. 72)
 - Good through degree 360 (111 km resolution)
 - EGM2008(EGM08)-produced by NGA
 - Much more refined solutions (incl. GRACE)
 - Good through degree 2160 (11 km resolution)







EGM's (continued)

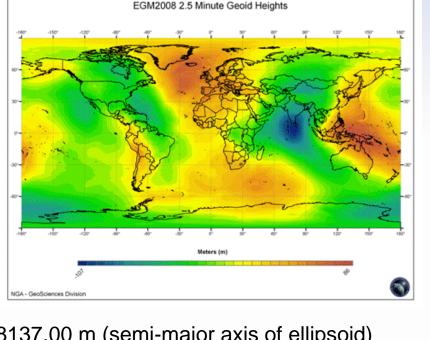
- Modeling is by inversion of EHM coefficients
- Harmonics are increasingly complex functions
- Applying a weight to these functions increases or decreases their power
- When added, the harmonics match the unique shape of the Earth's gravity field
- The trick then is to solve for the weights with the gravity observations and functions known (LSC)





EGM2008

- geoid undulation values with respect to WGS 84
- Tide-Free System
- NGA developing a WGS-84 ⇔ IGS08 transformation
- Nominally 5' (11 km) model
- Data in some regions is 15'
- Grids are available
- Can also get EHM coeff.



a=6378137.00 m (semi-major axis of ellipsoid)

f=1/298.257223563 (flattening of ellipsoid)

GM=3.986004418 x 10¹⁴ m³s⁻² (Product of the Earth's

mass & Gravitational Constant)

 ω =7292115 x 10⁻¹¹ radians/sec (Earth's angular velocity)







Regional Modeling

- General approach is to start from an EGM and refine using Remove-Compute-Restore Technique
- Gravity observations from multiple sources: terrestrial, shipborne, airborne, & altimetric
- NOTE: A lot of these same data went into EGM2008
- Must adopt an approach: Helmert vs. Molodensky
- Must account for terrain using RTM or TC
- Yields localized gravimetric geoid height model
- Does this match your vertical datum though?







Developing Regional Models

Molodensky

- Height anomalies
- Telluroid follows terrain
- Surface gravity anomalies
- No assumptions about ρ
- Russian approach from 60's
- Much more rigorous theory
- Inversion is very rough
- Popular in flatter countries
- Normal heights

Helmert

- Geoid heights
- Geoid approximates MSL
- "Downward" continued to MSL
- Must assume ρ to geoid
- Traditional approach
- Lots of assumptions required
- More rigor with adv. computing
- More consistent across mountains
- Helmert orthometric heights

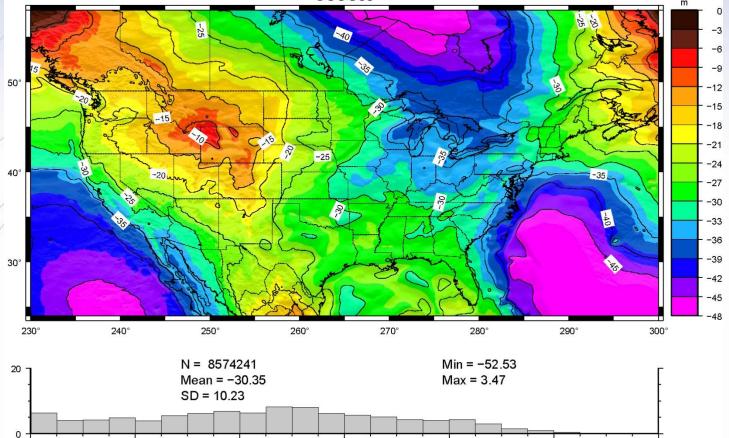






NOAA's National Geodetic Survey Positioning America for the Future U.S. Gravimetric Geoid for 2009

(USGG2009)



-24

(m)

-16



-48

-32

-8



World Height System vs. National Www.ngs.noaa.gov





Vertical Datums

- Recent efforts to realize a WHS have centered on use of EGM2008 or at least GRACE/GOCE
- However, this isn't acceptable to most National Cadastral Agencies with legacy Vertical Datums
- Movement is to adopt gravimetric geoid height models as basis for updated national vertical datums
- This would greatly facilitate development of a WHS since gravimetric geoids will likely be based on EGM2008 or GRACE/GOCE







Using a Geoid model as a National Vertical Datum

- This is easy iff the national level datum is actually consistent with geopotential surfaces
- Then the geoid model will be consistent, although a bias might be present
- What if the national level datum has a bias and a tilt (i.e., isn't an equipotential surface)?



SURVEY SURVEY

North American Vertical Datum 1988

(NAVD 88)

- Defined by one height (Father Point/Rimouski)
- Water-level transfers connect leveling across Great Lakes
- Adjustment performed in Geopotential Numbers
- Helmert Orthometric Heights:

$$-H = C/(g + 0.0424 H_0)$$

- -C = geopotential number
- -g = surface gravity measurement (mgals)
- $-H_0$ = approximate orthometric height (km)
- H = 0 level is nearly a level surface

Session 2.2: Gravity and WHS

 H = 0 level is biased and tilted relative to best available satellite-based geoid models











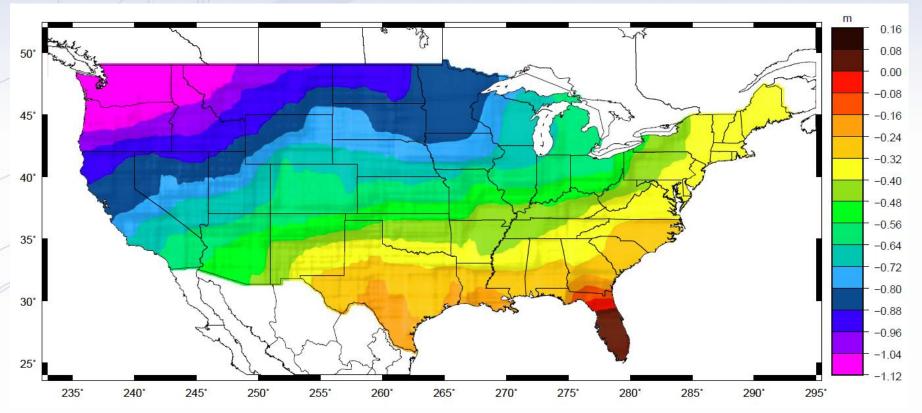
Figure 3. Vertical control used in 1988 adjustment.

450,000 BM's over 1,001,500 km





Why isn't NAVD 88 good enough anymore?



Approximate level of error known to exist in the NAVD 88 zero elevation surface







Hybrid Modeling Using Control Data and a Geoid Data and a Geoid Data and a Geoid



- Assumption is that the GNSS/leveling implied geoid height differs from the gravimetric geoid
 - $h H \neq N$

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- To a large extent, the above is never true
- If significant systematic biases exist, an alternative approach is required
- After creating the gravimetric geoid separately, it is warped to fit the level datum control data

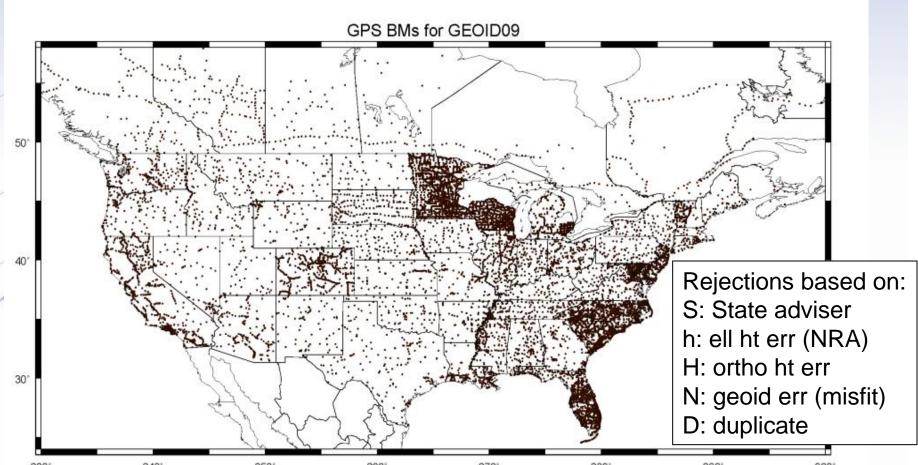


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GPSBM2009 (GEOID09 Control Data)



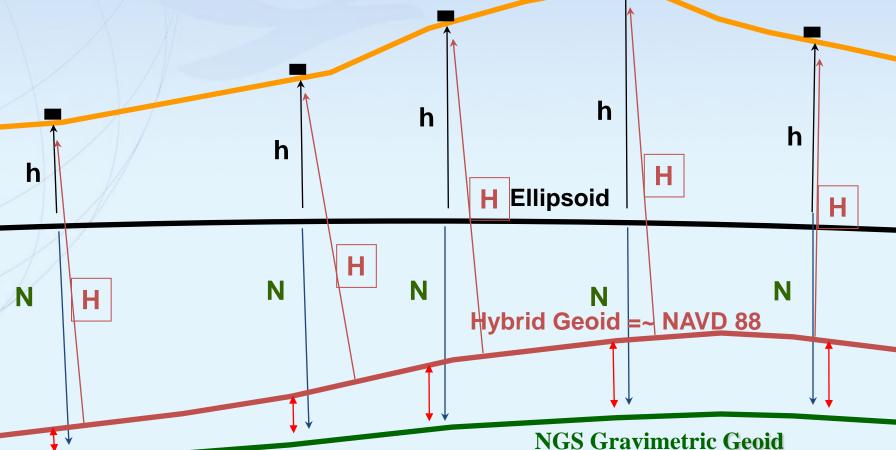
20446 total less **1003 rejected** leaves 18,867 (CONUS) plus 576 (Canada)



Earth's Surface



Hybrid Geoids



- Gravimetric Geoid systematic misfit with benchmarks
- Hybrid Geoid biased to fit local benchmarks
 - e = h H N







Official U.S. Datums

REGION	CONUS	Alaska	American Samoa	Guam	CNMI	Puerto Rico	US Virgin Islands
Ellipsoidal Reference Frame	NAD83 (NSRS 2007)	NAD83 (CORS96)	NAD83 (PACP00)	NAD83 (MARP00)	NAD83 (MARP00)	NAD83 (CORS96)	NAD83 (CORS96)
Vertical Datum	NAVD88	NAVD88	ASVD02	GUVD04	NMVD03	PRVD02	VIVD09

NAVD88 - NORTH AMERICAN VERTICAL DATUM OF 1988

ASVD02 - AMERICAN SAMOA VERTICAL DATUM OF 2002

GUVD04 - GUAM VERTICAL DATUM OF 2004

NMVD03 - NORTHERN MARIANAS VERTICAL DATUM OF 2003

PRVD02 - PUERTO RICO VERTICAL DATUM OF 2002

VIVD09 - VIRGIN ISLANDS VERTICAL DATUM OF 2009 -pending adoption







Future U.S. Vertical Datum

- U.S. will adopt a gravimetric geoid in 2022 $(USGG2022 \Rightarrow GEOID22)$
- GRAV-D combines GRACE, GOCE, aerogravity, terrestrial data, DEM, & DDM into a geoid model
- Already selected $W_0 = 62,636,856.00 \text{ m}^2/\text{s}^2$
- Canada will be adopting such a model in 2013
- U.S. and Canada will work to adopt a common North American Geoid and use for IGLD 15
- Use of GRACE/GOCE ties U.S. model to WHS



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Summary

- Gravity, geopotential, DoV's, and heights are all related functions of the Earth's gravity field
- In many instances, obtaining one type of data is sufficient for resolving all the others
- Hence, collecting gravity from space or in a plane can help determine heights on the ground
- Long wavelengths are best resolved by satellites
- This provides global consistency for all models



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Summary (cont.)

- GRACE and GOCE will likely resolve gravity field to degree 200 about 200 km scale features
- Terrestrial gravity can have systematic features that create dm- to m-level errors in the geoid
- The effects of the terrain must also be taken into account or risk making data look "noisy"
- Aerogravity provides means to bridge the gap between surface gravity and satellites gravity





Summary (cont.)

- Aerogravity can span across different environments (land and ocean)
- It can provide a seamless connection through gravity field across a continent and through middle of gravity spectrum
- DoV's can be derived from other observed data and yield better control for IMU's
- Earth Gravity Models, such as EGM2008, use all available data for a comprehensive reference model





Summary (cont.)

- Adoption of gravimetric geoids is the best means of improving accuracy of National Vertical Datums
- New Zealand has already done so; Canada will do so in 2013; the U.S. will do so in 2022
- Using a globally accepted reference field will best ensure a tie-in to a World Height System
- Regional geoid modeling will provide local refinements with a goal of cm-level accuracy

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Summary (cont.)

- Regional models can be built from EGM's
- These models provide basis for comparison to National Vertical Datums
- Involved procedures may be required to fit regional gravimetric geoids through control data
- This hybrid process keeps the character of the geoid between points while fitting to the Datum
- Systematic datum errors are preserved though







Thank you for your attention

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